Course: Advanced Mathematics/Text: <u>Advanced Mathematics</u>, by Richard G. Brown Standard: Numbers and Operations

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|--|---|--|--|
| M:N&O:AM:1 Demonstrates conceptual understanding of the real number system as an extension of the rational numbers by representing real numbers as infinite decimal expansions (that provide successive rational approximations to the number) and as points on a number line. | Real number system Rationals Irrationals As approximations to a number or as points on a number line | Presented as part of introductory unit/overview during the first two days of classes, p. 26 | Homework/graded homework/quizzes/chapter tests |
| Determines whether the decimal expansion of a rational number given in fractional form eventually repeats or terminates (without using a calculator). | Repeating rationals versus terminating | Included as introductory material during first two days of classes | |

Course: Advanced Mathematics Standard: Numbers and Operations,

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|--|---|-------------------------------------|--|
| Accurately solves problems. Solves problems involving scientific notation and assesses the precision of the answer in terms of significant digits. | Solves problems involving scientific notation | Page 267 problem 21 | Homework/graded homework/quizzes/chapter tests |
| Solves problems involving complex numbers by adding, | Complex numbers | pages 25-29 | |
| multiplying, dividing, and computing conjugates; interprets complex numbers | Complex Conjugates | page 25-29 | |
| geometrically; and understands complex numbers as an extension of the real numbers | Relationship to real numbers | pages 25-29 | |
| Manipulates complex numbers using rectangular and polar coordinates. Finds the <i>n</i> th roots of a complex number using De Moivre's | Rectangular coordinates and complex numbers | p 408, 493 | |
| Theorem. Solves compound interest problems including continuously compounded interest. | Compound interest and continuous compounding | p. 187-189 | |
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Course: Advanced Mathematics Standard: Numbers and Operations

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|---|--|-------------------------------------|--|
| M:N&O:AM:8 Explores field properties with vectors and matrices; | Vectors with matrices | p. 427 | Homework/graded homework/quizzes/chapter tests |
| algebraically/geometrically interpret vectors, vector | Vectors | p 419-421 | |
| addition, and scalar multiplication in the plane; | Vector addition | p 419-421 | |
| and solves problems using matrices (e.g., inverses, | Scalar multiplication | p 441 | |
| identity, determinants, and augmented matrices). | Determinants, inverses, identity matrices, augmented matrices | p 518, 531,530,523-525,530-532 | |

Course: Advanced Mathematics Standard: Geometry and Measurement

| Content | Activities | Assessments |
|---|---|---|
| | Resources & Materials | |
| Knowledge of proofs and proof techniques | Many problems in the problems sets contain proofs, or "show that." These problems are often included in the homework. | Homework/graded homework/quizzes/chapter tests |
| Coordinate proofs | p 214-217 | |
| Mathematical induction: | p. 510-512 | |
| Formulas for lengths of arcs | p. 263-264 | |
| Lengths of sectors | p 263-264 | |
| Areas of segments of circles | p. 263-264 | |
| Radian measure | Unit circle project, geometer's sketchpad unit on discovering radians. Use of applets on internet to | |
| Conversions Utility | demonstrate radian measure and unit circle Text pages 258-260 | |
| | Knowledge of proofs and proof techniques Coordinate proofs Mathematical induction: Formulas for lengths of arcs Lengths of sectors Areas of segments of circles Radian measure Conversions | Resources & MaterialsKnowledge of proofs and proof techniquesMany problems in the problems sets contain proofs, or "show that." These problems are often included in the homework.Coordinate proofsp 214-217Mathematical induction:p. 510-512Formulas for lengths of arcsp. 263-264Lengths of sectorsp 263-264Areas of segments of circlesp. 263-264Radian measure ConversionsUnit circle project, geometer's sketchpad unit on discovering radians. Use of applets on internet to demostrate radian measure and unit circle Text pages 258-260 |

Course: Advanced Mathematics Standard: Geometry and Measurement

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|---|------------------------------------|-------------------------------------|--|
| M:G&M:AM:9 Solves problems using analytic geometry (including three- dimensions) and circular | Analytic geometry applications | p. 213-218 | Homework/graded homework/quizzes/chapter tests |
| trigonometry (e.g., find the equation of a circle inscribed in a triangle; find the distance | Circular trigonometry applications | p 219-222, p 224 # 47 | |
| between opposite vertices in a rectangular solid); | Rectangular solids | | |
| explores and interprets the characteristics of conic | Conics | p 225-229, p 231-242 | |
| sections graphically and algebraically including understanding how different | Graphically and algebraically | p 247-252, p 456 | |
| planar slices of a double cone yield different conic sections; knows the characterization of conic sections as loci of | Characteristics of conics | p .252 | |
| points in the plane satisfying certain distance requirements, and uses the distance formula to obtain equations for the conic sections. | Distance formula applications | p. 4, p. 219-229 | |
| | | | |

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|---|--|---|--|
| M:F&A:AM:1 Computes partial sums of infinite arithmetic and geometric sequences, determines when an infinite geometric series converges, and finds its sum. Connects arithmetic and geometric sequences to linear and exponential functions, respectively. Works between recursive and explicit representations. | Geometric sequences Partial sums Infinite geometric series convergence and their sums Connection of arithmetic and geometric sequences to linear/exponential functions Recursive/explicit representations | p. 473 p. 181, 473-481,500 p. 493-496, 500, 501,502 p. 486, 487,488 p 486-488 | Homework/graded homework/quizzes/chapter tests |

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|--------------------|--|-------------------------------------|---|
| | Linear versus nonlinear | Pages 1-4, 7-10,14-16,19-22. | Homework/graded homework/quizzes/chapter tests |
| | Definition of functions | Pages 1-4, 7-10,14-16,19-22. | |
| | Operations of functions | Pages 124-127 | |
| | Composition of functions | p. 126 | |
| | Algebraic to numeric to graphic representation | pgs. 1-22 | |
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| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|---|---|-------------------------------------|--|
| M:F&A:AM:3 Conceptual understanding of algebraic expressions. | | | Homework/graded homework/quizzes/chapter tests |
| Simplifies complex fractions. | Simplify complex expressions | рр. 169-172 | |
| Uses the Remainder Theorem, the Factor Theorem and Rational Root Theorem for polynomials. | Remainder, Factor, Rational Root theorems | pp. 59, 60, 82, | |
| Knows the Fundamental Theorem of Algebra and that non-constant polynomials always factor into linear | Fundamental theorem of algebra | p. 85 | |
| factors over the complex numbers. | Factoring non- constant polynomials | pp. 80-83 | |
| Understands the difference between factoring polynomials over integer, rational, real, and complex numbers. | Factoring polynomials | рр. 59-60 | |

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|---|---|---|--|
| M:F&A:AM:4 Demonstrates conceptual understanding of equality. Solves equations and verifies/proves identities involving trigonometric | Trigonometric identities Proving/verifying identities/solve | P 317-326 p. 318-320, problems and handouts that contain identities | Homework/graded homework/quizzes/chapter tests |
| expressions. Solves equations involving exponential and logarithmic expressions; graphs and interprets the solutions. Uses matrices or determinants to solve systems of equations with or without technology. Knows and applies the Intermediate Value Theorem to find exact or approximate solutions of equations or zeros of continuous functions. | equations Exponential functions Inverses Graphs Solutions of equations matrices to solve equations Intermediate value theorem and application, or the location principle | p. 180-182, 187-189, 184, 183, 170 p. 191-209 p. 518, 530-533, activities include using TI-83 and inverse matrices to solve 2x2 and 3x3 simultaneous equations p. 76 | |

Course: Advanced Mathematics Standard: Data, Statistics, and Probability

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|--------------------|---|--|--|
| | Standard deviation Variance Percentiles | p. 653-657, 674-677 | Homework/graded homework/quizzes/chapter tests |
| | Measures of central tendency | p. 639-642 | |
| | Correlation coefficient Coefficient of determination | p 660-665 | |
| | Method of least squares | p. 684, these problems use a graphing calculator | |
| | Median median for linear regression | p. 830-834, these problems use a graphing calculator | |
| | | | |

| Knowledge & Skills | Content | Activities | Assessments |
|--|---|--|--|
| | | Resources & Materials | |
| Analyzes characteristics of classes of functions and inverse functions | Exponential functions Domain/range/characteristics | pp. 180-182, 20, 119, TI-83 activity | Homework/graded homework/quizzes/chapter tests |
| (exponential, logarithmic, trigonometric) to include | Logarithmic functions | p. 191-209, handout on acidity and logs | |
| domain, range, intercepts, increasing and decreasing | Domain/range/characteristics | handout on logarithmic functions and rules | |
| intervals and rates of change, periodicity, end behavior, maximum and minimum | Trigonometric functions Domain/range/characteristics | p 256-293 | |
| values, continuity, and asymptotes; graphs classes of functions; and understands | Intercepts | p. 221, 2-3 | |
| domain restrictions and their effects on functions. | Periodicity | p. 138-142 | |
| | Rates of change | p. 7-10 | |
| | End behavior | p. 62-65 | |
| | Maximum and minimum values | p. 68-70 | |
| | | Each of these topics has a technology exploration in the text which uses a graphing calculator. Geometer's sketchpad lessons aare also available | |

| Knowledge & Skills | Content | Activities | Assessments |
|--|-----------------------------------|---|--|
| | | Resources & Materials | |
| Analyzes properties of functions including onto (surjectivity), critical points and | Asymptotes | p. 232 | Homework/graded homework/quizzes/chapter tests |
| inflection points. Determine graphically and analytically whether a function is even, odd or neither. | Critical points | p. 166 in Larson, <u>Calculus of a Single Varible</u> | |
| Analyzes informally the idea of continuity and limits. | Inflection points | p. 192, 193 in Larson. | |
| | Even versus odd versus neither | p. 137-138 | |
| | Limits | pp. 45,48,52,59,60,63 in Larson | |
| | Definition | p. 52 in Larson | |
| | Existence | p. 73 in Larson | |
| | Limits and continuity | p. 70,73 in Larson | |
| | Right and left handed limits | p. 83 in Larson | |
| | | | |

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|---|--|-------------------------------------|-------------|
| Understanding quadratics and quadratic applications | Graphing quadratics | p. 37 | |
| | Finding zeros and the discriminant | p. 38-39 | |
| | Intersection of quadratics and linears | p. 40 | |
| | The quadratic formula | p. 31 | |
| | Complete the square | p. 31 | |
| | Factor | | |
| | Graphing | p. 38 | |
| | Significance of max or min | p. 38-39 | |
| | Real versus imaginary roots | p. 31-40 | |
| | | | |

| Knowledge & Skills | Content | Activities | Assessments |
|----------------------------|------------------------|--|----------------------|
| - | | Resources & Materials | |
| Finding limits graphically | Concept of limit | Textbook: Larson, Hostetler, Calculus of a single | Homework completion |
| and analytically | | Variable, 9 th edition | assessment, assessed |
| | How to find a limit | Teacher-led instruction | homework |
| | | Chapter 1.2 | Quizzes/tests |
| | | | Calculator problems |
| | Numerical | Find a limit numerically by creating a table | |
| | approximations | Chapter 1.2 | |
| | Properties of limits | Calculate the limit of a sum, difference, product and quotient of a function | |
| | Limits of | Chapter 1.3 | |
| | trigonometric | 1 | |
| | functions/one sided | Examine infinite limits graphically, numerically, and | |
| Continuity | limits, asymptotes | algebraically. Use the concept of infinite limit to find | |
| | | vertical asymptotes, Chapt 1.3, p 61 | |
| | Infinite Limits | p. 205 | |
| | | Use a graphing calculator to find the limit of a function | |
| | Definition of | from both the tables and from the graph | |
| | continuity, continuity | | |
| | of functions, and the | Find when a limit does not exist | |
| | properties of | | |
| | functions. | | |
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| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
|---|--|---|---|
| Students will have an understanding of the Intermediate Value Theorem (ITV). | Definition of the ITV The relationship between the tangent line and slope | Use the definition of continuity to determine whether a function is continuous at a point or on an interval, chapt 1.3 Find points of discontinuity for a function | Homework completion assessment, assessed homework Quizzes/tests Calculator problems |

Course:

| Knowledge & Skills | Content | Activities Resources & Materials | Assessments |
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